2016

PHYSICS

(Major)

Paper : 2.1

Full Marks: 60

Time: 3 hours

The figures in the margin indicate full marks for the questions

GROUP-A

(Mathematical Methods-II)

(Marks: 35)

1. Answer the following questions:

1×4=4

- (a) Find the value of \vec{r} satisfying the equation $\left(\frac{d^2\vec{r}}{dt^2}\right) = a$.
- (b) What are the coordinate surfaces in cylindrical coordinates?
- (c) Find the value of $\Gamma(0)$.
- (d) Evaluate: $\int_{2}^{6} (3x^{2} 2x 1) \delta(x 3) dx$

- 2. Answer the following questions:
- 2×3=6
- (a) Find the total work done in moving a particle in a force field given by $\vec{F} = 3xy\hat{i} 5z\hat{j} + 10x\hat{k}$ from t = 1 to t = 2.
- (b) Define Gamma function and Dirac delta function.
- (c) Show that $\iint_S \vec{A} \cdot \hat{n} \, dS$, over any closed surface S is equal to $\iint_R \vec{A} \cdot \hat{n} \, \frac{dx \, dy}{|\hat{n} \cdot \hat{k}|}$, where R is the projection of S on xy-plane.
- 3. Answer any two of the following questions:

- (a) If $\overrightarrow{F} = (2x^2 3z)\hat{i} 2xy\hat{j} 4x\hat{k}$, then evaluate $\iiint_V \overrightarrow{F} dV$, where V is the region bounded by the planes x = 0, y = 0, z = 0 and 2x + 2y + z = 4.
 - Show that in orthogonal coordinates $\overrightarrow{\nabla} \times (A_1 \hat{e}_1) = \frac{\hat{e}_2}{h_3 h_1} \frac{\partial}{\partial u_3} (A_1 h_1) \frac{\hat{e}_3}{h_1 h_2} \frac{\partial}{\partial u_2} (A_1 h_1)$ where symbols have their usual meanings.
- (c) Show that $\Gamma(n) = (n-1)\Gamma(n-1)$ for all values of n and $\Gamma(n) = (n-1)!$, when n is a positive integer.

4. Answer any one of the following:

- 4
- (a) Verify divergence theorem for the vectors $\vec{V} = x^2\hat{i} + y^2\hat{j} + z^2\hat{k}$, taken over the cube 0 < x, y, z < 1.
- (b) Prove that a spherical coordinate system is orthogonal.
- **5.** Answer any *three* questions from the following: 5×3=15
 - (a) Show that—
 - (i) $\delta(-x) = \delta(x)$
 - (ii) $x\delta'(x) = -\delta(x)$

- 2+3=5
- (b) Show that $\iint_{S} (\vec{\nabla} \times \vec{A}) \cdot \hat{n} dS = \oint_{C} \vec{A} \cdot d\vec{r}$
- (c) Express $\nabla^2 \psi$ in orthogonal curvilinear coordinates.
- (d) If S be a closed surface and \vec{r} denotes the position vector of any point (x, y, z) measured from an origin O, prove that $\iint_{S} \frac{\hat{n} \cdot \vec{r}}{r^3} dS \text{ is equal to } 4\pi \text{ if } O \text{ lies inside } S.$
- (e) Find the circulation of F round the curve C, where

$$\vec{F} = e^x \sin y \hat{i} + e^x \cos y \hat{j}$$

and C is the rectangle whose vertices are (0, 0), (1, 0), $(1, \frac{\pi}{2})$ and $(0, \frac{\pi}{2})$.

GROUP-B

(Properties of Matter)

(Marks : 25)

6. Answer the following questions:

1×5=5

- (a) Why is a hollow shaft of the same material, mass and length very much stronger than that of a solid shaft?
- (b) What is the velocity profile of a advancing liquid through a horizontal capillary tube?
- (c) When is the surface energy of a liquid surface equal to the surface tension?
- (d) Write the expression for excess pressure of cylindrical bubble in a liquid.
- (e) Write the expression for time period of a torsional pendulum.
- 7. Answer either (a) and (b) or (c) and (d): 10

Either

(a) Find an expression for energy per unit volume of a stretching wire. Show that a shear is equivalent to a compression and an extension.

3+3=6

(b) A bronze bar, 1.7 m long and 50 mm in diameter is subjected to a tensile stress of 70 meganewton/m². Calculate the extension produced in the bar and the work done during the process. The value of Young's modulus for the material of the bar may be taken to be 85×10⁹ N/m².

Or'

- (c) Calculate the depression at the free end of a thin light beam, clamped horizontally at one end and loaded at the other.
- (d) For the same cross-sectional area, show that a beam of square section is stiffer than that of a circular section of same material. Show also for a given load the depressions are in the ratio 3:π.
- 8. Answer any two questions of the following:

5×2=10

(a) Show that shearing stress at a point in a twisted cylinder or a wire depends on the distance of the point from the axis and not its vertical distance from either end of it.

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- (b) The rate of flow of liquid through a capillary is given $Q = \frac{\pi P r^4}{8\eta l}$ with usual notations. Deduce this relation stating clearly the conditions under which it holds. Why does the formula fail in the case of tube of wide bore? 4+1=5
- (c) (i) For a homogeneous isotropic substance, show that $\frac{Y}{\eta} = 2(\sigma + 1)$, where symbols have their usual meanings.
 - (ii) A gold wire 0.32 mm in diameter elongated by 1 mm, when stretched by a force of 330 gm-wt and twists through 1 radian, when equal an opposite torque of 145 dyne-cm are applied at its end. Find the value of Poisson's ratio for gold.

 3+2=5
- (d) (i) Show that excess pressure acting on a curved surface of a curved membrane is given by

$$P = 2T\left(\frac{1}{r_1} + \frac{1}{r_2}\right)$$

where r_1 and r_2 are the radii of curvature and T the surface tension of the membrane.

(ii) Two equal spherical soap bubbles coalesce to form one spherical soap bubble without any leakage of air. If V is the consequence change in volume of the contained air and S, the change in the total surface area, show that 3PV+4ST=0, where T is the surface tension of the soap bubble and P, the atmospheric pressure.

2016

PHYSICS

(Major)

Paper: 2.2

Full Marks: 60

Time: 3 hours

The figures in the margin indicate full marks for the questions

1. Answer the following questions:

1×7=7 <

- (a) At what temperature in centigrade scale, the platinum scale temperature coincides with centigrade scale?
- (b) What is the value of $\int_0^\infty F \, dc$, where F = Maxwell's velocity distribution function and integration is taken w.r.t. c, for all possible velocities of gas molecules?
- (c) Which physical quantity remains constant during an adiabatic process?
- (d) What is triple point?

- (e) State Carnot's theorem of heat engine.
- (f) What is Brownian motion?
- (g) Why are two specific heats defined for gases?
- 2. Answer the following questions:



- (a) Calculate the value of R using the relation PV = RT.
- (b) Using Maxwell's velocity distribution law, deduce the expression of root-mean-square velocity of gas molecules of an ideal gas.
- (c) Calculate the work done during isothermal expansion from volume V_1 to V_2 of a van der Waals' gas.
- (d) From Planck's law of radiation, deduce Rayleigh-Jeans law.
- (e) The specific volumes of water and steam at $100 \, ^{\circ}\text{C}$ and $760 \, \text{mm}$ of Hg pressure are $1 \, \text{cc/gm}$ and $1601 \, \text{cc/gm}$ respectively and $L = 536 \, \text{cal/gm}$. Calculate the change in the boiling point of water due to a pressure change of $1 \, \text{cm}$ Hg.



(f) Write four defects of van der Waals' equation of state.

3. Answer any four of the following:

5×4=20

(a) Derive an expression of pressure of ideal gas using kinetic theory of gases.

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(b) A cylindrical tube of radii 1 cm and 4 cm has temperatures θ_1 and θ_2 at the inner and outer surfaces respectively. Find at what distance from the axis, the temperature will be $\frac{\theta_1 + \theta_2}{2}$.

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(c) Explain the meaning of entropy. One mole of perfect gas is changed from P_1 , V_1 , T_1 to P_2 , V_2 , T_2 . Show that the change in entropy

$$\Delta S = C_V \log_e \frac{P_2}{P_1} + C_P \log_e \frac{V_2}{V_1}$$
1+4

(d) Write the four Maxwell's equations in thermodynamics. Using these equations, prove

$$C_P - C_V = T \left(\frac{dP}{dT}\right)_V \left(\frac{dV}{dT}\right)_P$$
 2+3

(e) Derive Wien's radiation law.

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4.	Answer	any	three	of	the	following	: 195 20	7×3=21
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- (a) Derive the expression of mean free path using Maxwell's velocity distribution law.
- (b) Deduce the general equation of transport phenomena. From this equation, derive the expression of coefficient of viscosity.

 5+2
- (c) Describe Andrews' experiment. What are the inferences drawn from this experimental results? 4+3
- (d) State the first law of thermodynamics. Write its limitations. Explain how from efficiency of Carnot's engine the second law of thermodynamics can be derived and how it explains the limitation of first law. Also, explain the second law in terms of entropy.

 1+2+2+1+1
- (e) How do you account theoretically for pressure of radiation? Give a method to determine it experimentally.

 4+3

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